

سیستم زیر را به کمک محیط سیمولینک شبیه‌سازی و با فرض ورودی پله شبیه‌سازی کنید.

توجه: سیگنال بار TL در ثانیه ۱۰ از مقدار ۵۵ به مقدار ۱۱۰ تغییر می‌کند.

## 2. MOTOR DYNAMICS

Consider a series DC motor shown in Figure 1 below.

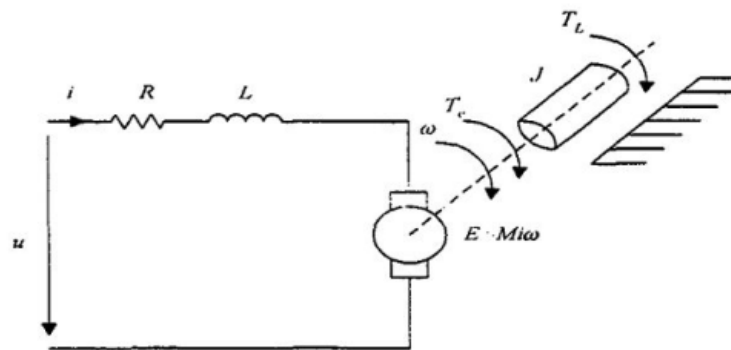


Fig. 1. Series DC motor

If we neglect magnetic saturation in field circuit, the motor can be modeled as (refer to Liu et al. (1999) for details).

$$\begin{aligned} L \frac{di}{dt} &= u - Ri - Mi\omega, \\ J \frac{d\omega}{dt} &= Mi^2 - T_L, \end{aligned} \quad (1)$$

where the physical meaning of the quantities are as follows.

$i$ : armature current (or field current)

$u$ : terminal control voltage

$\omega$ : rotational speed of the motor

$L$ : total armature and field current inductance

$R$ : total armature and field circuit resistance

$J$ : moment of inertia associated with both motor and the load



$M$ : motor constant

$T_L$ : load torque

$$T_e = Mi^2 \text{ and } E = Mi\omega.$$

For notational convenience, we set

$$x_1 = \omega, x_2 = i.$$

Then, the system (1) becomes

$$\begin{aligned} \frac{dx_1}{dt} &= \frac{M}{J}x_2 - \frac{T_L}{J}, \\ \frac{dx_2}{dt} &= -\frac{1}{L}(Rx_2 + Mx_1x_2) + \frac{1}{L}u. \end{aligned} \quad (2)$$

The control goal is to design a feedback controller  $u$  such that the speed of the motor  $x_1$  tracks a constant desired speed  $\omega_r$ .

$$\begin{aligned} R &= 1\Omega, & J &= 0.5\text{kgm}^2, \\ L &= 0.05\text{H}, & M &= 0.027\text{H}, \\ T_L^1 &= 55\text{Nm}, & T_L^2 &= 110\text{Nm} \\ \omega_r &= 151.7. \end{aligned}$$